

# CSE 231: Closures

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## Closures

In a few steps, we will extend our language with the ability to treat functions as first-class values.

1. Labels
2. Anonymous functions
3. Arity
4. Free Variables
5. Recursion

## Part 1: Functions as Values

### QUIZ: Semantics

What should the following code evaluate to?

```
(fun (f it)
  (it 5))

(fun (inc x)
  (+ x 1))

(f inc)
```

## Abstract Syntax

```
pub struct Defn {
  name: String,
  params: Vec<String>,
  body: Expr,
}

pub enum Expr { ...
  Fun(Defn),
}
```

## Parser

No need for Prog! But need to change the parser, to produce a single Expr instead of a Prog.

```
fn prog(defns: Vec<Defn>, e: Expr) -> Expr {
  ...
}
```

## Evaluator

The type of Val is extended to include Fun

```
pub enum Val { ...
  Fun(Defn),
}
```

### QUIZ: Extend eval to remove funs

```
fn eval(&self, e: &Expr, env: &mut Env) -> Val {
  match e {
    ...
    Expr::Defn(defn) =>
      _____,
    Expr::Call1(f, e1) => {
      let v1 = eval(e1, env)?;
      _____
      _____
      _____
      _____
    }
    ...
  }
}
```

### QUIZ: Compiler: Fun Call

```
Fun(defn) => self.compile_defn(defn),
```

```
Call1(f, e1) =>
```

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**Compiler: Fun Definition**

```
fn compile_defn(&mut self, defn: &expr::Defn) ->
String {
    let name = defn.name.clone();
    // labels
    let entry_label = entry_label(&name);
    let finish_label = finish_label(&name);
    let body_label = body_label(&name);
    // setup, body, exit
    let entry = compile_entry(&defn.body);
    let stack = Stack::new(&defn.params[..]);
    let body = self.compile_expr(&defn.body, &stack,
    &exit_label());
    let exit = compile_exit();
    // code
    format!(
        "jmp {finish_label}\n\
        {entry_label}:\n\
        {entry}\n\
        {body_label}:\n\
        {body}\n\
        {exit}\n\
        {finish_label}:\n\
        lea rax, [rel {entry_label}]"
    )
}
```

**QUIZ: Stack Allocation**

What is `max_vars` for a `Defn`?

**Part 2: Anonymous functions**

Since fun are also let-bound values, we can just use `let` to name them. So we can write:

**QUIZ: Semantics**

What should the following code evaluate to?

```
; anon function that takes `it` and returns `it 5`
(let (f (fn (it) (it 5)))

; anon function that takes `z` and returns `( + z 1 )`
(let (inc (fn (z) (+ z 1)))

    (f inc)

))
```

## Abstract Syntax

We just need to support **nameless** definitions, so we can reuse `Defn` with an optional name.

```
pub struct Defn {
  name: Option<String>,
  params: Vec<String>,
  body: Expr,
}
```

Update the parser to support `fn` as well as `fun...`

Evaluation, Compilation is unchanged!

### Part 3: Arity

But wait a minute... what if we call a function with the wrong number of arguments?

**QUIZ: Semantics** What should the following code evaluate to?

```
(let (f (fn (it) (it 5)))
  (let (add (fn (x1 x2) (+ x1 x2)))
    (f add)
  ))
```

### Representation

Have to track the *arity* of each function, i.e. the number of parameters it takes.

Store a **function value** as **pointer** to a `Vec`-like structure

- arity (at [offset 0])
- code-label (at [offset 8])

```
[fun-arity][fun-label]
```

**Problem** need to *distinguish* this from *other* values, e.g. `int` or `bool` or `vec`!

### Tags

Modify tagging scheme for `vec` to use the `0101` tag for function values.

Leaves **other** types unchanged.

Value	Representation
number	<code>xxx0</code>
false	<code>x011</code>

```

true          x111
nil           1001
(vec ...)     0001
(fun ...)     0101

```

## Runtime Types

```

pub enum Ty { ...
    Fun,
}

const CLOSURE: i64 = 5;

fn test_type(ty: Ty) -> String {
    let (mask, expected) = match ty {
        Ty::Num => (0b1, 0),
        Ty::Bool => (0b11, 3),
        Ty::Vec => (0b111, 1),
        Ty::Fun => (0b111, 5),
    };
    format!(
        "mov rcx, rax\n\
         and rcx, {mask}\n\
         cmp rcx, {expected}\n\
         mov rcx, {code}\n\
         cmovne rdi, rcx\n\
         jne label_error"
    )
}

```

## Compiler: Call

```

fn compile_callee(f: &String, arity: usize) ->
String {
    ...
    format!(
        "; load closure point\n\
         mov rax, [rbp - 8*{f_pos}]\n\
         {check_closure}\n\
         ; strip tag\n\
         mov rcx, rax\n\
         sub rcx, {CLOSURE}\n\
         ; check arity\n\
         mov rcx, [rcx]\n\
         cmp rcx, {arity}\n\
         mov rdx, 77\n\
         cmovne rdi, rdx\n\
         jne label_error")
    }
}

```

```
)
}
```

```
fn compile_expr(e: &Expr, stack: &Stack) -> String {
  match e {
    Call1(f, e1) => {
      let e1_code = self.compile_expr(e1, stack, ...);
      let f_code = self.compile_callee(f, stack, 1);
      format!(
        "{e_code}\n\
        push rax\n\
        {f_code}\n\
        sub rax, {CLOSURE}\n\
        call rax\n\
        add rsp, 8")
    }
  }
}
```

### Compiler: Definition

```
fn compile_defn(&mut self, defn: &expr::Defn) ->
String {
  "jmp {finish_label}\n\
  {entry}\n\
  {body_label}:\n\
  {body}\n\
  {exit}\n\
  {finish_label}:\n\
  ; write arity \n\
  mov rcx, {arity}\n\
  mov [r11], rcx\n\
  ; write label \n\
  lea rcx, [rel {entry_label}]\n\
  mov [r11 + 8], rcx\n\
  ; set closure address\n\
  mov rax, r11\n\
  add r11, 16\n\
  add rax, {CLOSURE}"
}
```

### *Part 4: Free Variables*

### *Part 5: Recursion*